

MALLA REDDY COLLEGE OF ENGINEERING & TECHNOLOGY

(Autonomous Institution – UGC, Govt. of India)

II B.Tech II Semester Regular/Supplementary Examinations, July 2023

Probability & Random Processes

(ECE)

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Time: 3 hours**Max. Marks: 70**

Note: This question paper Consists of 5 Sections. Answer **FIVE** Questions, Choosing **ONE** Question from each **SECTION** and each Question carries 14 marks.

SECTION-I

Marks

- 1 **A** Explain about various types of sets and operations on sets in detail **[7M]**
 B An ordinary 52-card deck is thoroughly shuffled and 4 cards are drawn **[7M]**
 then what is the probability that all 4 cards are sevens?

OR

- 2 **A** Explain various types of events with necessary examples. **[7M]**
 B A machine gun fires 3 sec at the rate of 2400 bullets/minute. The **[7M]**
 probability of hitting the target is 0.4. Estimate the probability of exactly
 50 bullets hitting the target.

SECTION-II

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|----------|----------|---|-------------|
| 3 | A | Explain the operations expected value and variance of single random variable in detail. | [7M] |
| | B | The mean & variance of Binomial Distribution are 6 & 2.4 respectively. Find $p\{X>2\}$ | [7M] |

OR

- 4 **A** Describe with necessary expression about the properties of probability density function. **[7M]**
- B** Find the probability that if tossing a fair coin 5 times then there will be appear
 a) 3 heads b) 3 tails and 2 heads c) at least 1 head d)
 not more than one tail **[7M]**

SECTION-III

- | | | | |
|---|----------|---|-------------|
| 5 | A | Define and state the properties of joint density function and joint Distribution function | [7M] |
| | B | Explain statistical independence of the random variables. | [7M] |

OR

- 6** **A** The joint density function of random variables X and Y is **[7M]**

$$f_{x,y}(x,y) = 4xye^{-(x^2+y^2)}u(x)u(y) f(y/x) \text{ and } f(x/y)$$
- B** The joint probability density function is **[7M]**

$$f_{x,y}(x,y) = 1/24 \quad 0 < x < 6, 0 < y < 4$$

$$= 0 \quad \text{elsewhere}$$

Find the expected value of the function $g(X,Y)= (XY)^2$

SECTION-IV

- 7 A Differentiate random variable and random process. [7M]

- B** A random process $Y(t)$ is given as $Y(t)=X(t)\cos(\omega t+\Theta)$, where $X(t)$ is a wide sense stationary random process , ω is constant and Θ is random variable independent on $X(t)$, uniformly distributed on $(-\pi,\pi)$. Find a) $E[Y(t)]$ b) $R_{YY}(\tau)$. [7M]

OR

- 8** **A** Define LTI system and derive the expression for following for the response of LTI system. [7M]
a) Mean b) Auto correlation function c) Cross correlation
B State and prove the properties of auto correlation function. [7M]

SECTION-V

- 9** **A** Define power spectral density and state and prove its properties. [7M]
B A random process $Y(t)$ has the power spectral density $S_{YY}(\omega)=9/\omega^2+64$ Find the Auto correlation function of $Y(t)$. [7M]

OR

- 10** **A** Derive the cross PSD between input and output of an LTI system [7M]
B Find the PSD of WSS random process $X(t)$ whose auto correlation function is $R_{XX}(r) = ae^{-b|r|}$ [7M]
